### Debt and Inflation

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# CBO US Debt Forecast



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# MV = PY

How is 100% Debt/GDP sustainable?

$$(r - g)\frac{D}{Y} = \frac{S}{Y}$$
  
(interest - growth rate)  $\times \frac{\text{Debt}}{\text{GDP}} = \frac{\text{Surplus}}{\text{GDP}}$   
Was : (5% - 4%)  $\times 100\% = 1\%$   
US,UK : (1% - 0%)  $\times 100\% = 1\%.(-10\%?)$   
Next? : (5% - 0%)  $\times 100\% = 5\%?(-10\%?)$ 

Answer: Growth

### Output in the 1980s and now



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Source: John Taylor

#### What will it look like?

Debt is the present value of future surpluses

$$\begin{array}{lcl} \displaystyle \frac{D_t}{P_t} & = & E_t \sum_{j=0}^\infty \frac{1}{R^j} S_{t+j} \\ \\ \displaystyle \frac{\text{Debt}}{\text{Price Level}} & = & \text{Expected Discounted Future Surpluses} \end{array}$$

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Bad news about the future leads to inflation or default today.

# **Policy Options**

Where do surpluses come from

$$\begin{array}{lll} \displaystyle \frac{D_t}{P_t} & = & E_t \sum_{j=0}^{\infty} \frac{1}{R^j} S_{t+j} = E_t \sum_{j=0}^{\infty} \frac{1}{R^j} \left[ \tau \ (1+g)^j \ Y_t - G_{t+j} \right] \\ \\ \displaystyle \frac{\text{Debt}}{\text{Price Level}} & = & \text{Expected Discounted Future Surpluses} \\ \\ & \text{Surplus}_{t+j} & = & (\text{tax rate } \times \text{ growth}^j \ \times \ \text{GDP - spending}) \end{array}$$

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#### What are the options?

- 1. Austerity
- 2. Stimulus
- 3. Growth

# Surplus and GDP



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Detrended GDP = GDP - last 10 year trend line.