

# Human Capital Accumulation, Private Information, and Insurance

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# Introduction

- Q: How does Human Capital (HC) accumulation interact with Insurance Markets?
- Human Capital delivers stochastic returns (e.g, Carneiro-Cuhna-Hansen-Heckman-Navarro...).
  - ① How incomplete insurance markets affect HC accumulation?
  - ② Is there scope for public intervention? If yes, how?
- Focus on **Insurance of HC risk** (not on liquidity)
- Review of a selected literature;
- Discuss how answers depend on the nature of markets: exogenously vs endogenously incomplete markets.

# Literature

- Exogenous Markets and Linear Taxes
  - Eaton & Rosen (1980), Hamilton (1987), Aiyagari (1995)
  - Anderberg & Andersson (2003) and Jacobs et al. (2010), Pavoni & Gottardi (2012), Gottardi et al. (2012)
- Endogenously Incomplete Markets and/or Optimal Taxation
  - da Costa & Maestri (2007), Anderberg (2009), Grochulski & Pirsorski (2006)
  - Kapicka (2006-2010-2012), Abraham et al. (2012)
  - Bovenberg & Jacobs (2005-2008), Bohaceck & Kapicka (2008), Findeisen & Sachs (2011)

# The Working Model

## Technology and Preferences

- Agents face idiosyncratic shocks (health/job/disability):

$$\tilde{\theta} \in \{\theta, 0\} \quad \text{where } \theta > 0 \quad \text{with prob. } \pi.$$

- Agents live two periods;
- At  $t = 0$  they invest in HC; in  $t = 1$  they work
- Fixed inter-temporal transfer technology  $1 \Rightarrow 1/q$
- Labor income is given by  $y = w(h_0)\tilde{\theta}l_1$ , with  $w'(h_0) \geq 0$ .
- Preferences over consumption, HC and labor  $(c_0, h_0, c_1, l_1)$  :

$$u(c_0 - h_0) + \beta [u(c_1) - v(l_1)].$$

$p = 1$  price of HC;  $u$  concave,  $v$  convex (strictly),  $v(0)=0$ .

# Market Arrangements

# Complete Markets (First Best)

Assume that all actions are public information

$$\begin{aligned} & \max_{c_0, h_0, c(\theta), \underline{c}, l(\theta) \geq 0} u(c_0 - h_0) + \beta\pi [u(c(\theta)) - v(l(\theta))] + \beta(1 - \pi)u(\underline{c}) \\ & \text{subject to} \\ & y_0 - c_0 + q\pi [w(h_0)\theta l(\theta) - c(\theta)] - q(1 - \pi)\underline{c} \geq 0. \quad (\lambda) \end{aligned}$$

- 1 Full-Insurance:  $c(\theta) = \underline{c} = c_1^*$
- 2 Production efficiency:  $\theta w(h_0^*)u'(c_1^*) = v'(l^*(\theta)), l(0) = 0$
- 3 Intertemporal efficiency:  $qu'(c_0^* - h_0^*) = \beta u'(c_1^*) = q\lambda$
- 4 HC investment optimality:

$$\frac{1}{q} = \pi w'(h_0^*)\theta l^*(\theta).$$

# Policy Concepts and Terminology

- 1 First-Best **social returns** can be compared to social returns in imperfect economies. Is it a useful concept?
- 2 First-Best **social margins** can be compared to social margins in imperfect economies; perhaps more useful.
- 3 For each economy, one can compare **social margins vs private margins**  $\Rightarrow$  **wedges**.
- 4 In general, **(linear) taxes differ from wedges**.
  - They are the same only in concave economies
  - Wedges inform on '**third-best**' **linear taxes** in non-concave economies (Ramsey)



## Private Margins and Wedges

- Now we ask: **is the agent at his/her private optimum?**
- Private and social margins for savings coincide:

$$qu'(c_0^* - h_0^*) = \beta u'(c_1^*)$$

- As they do for labor supply:

$$\theta w(h_0^*) u'(c_1^*) = v'(l^*(\theta)), \quad l(0) = 0.$$

- **Private margin for HC investment is also aligned** to social margin:

$$\frac{1}{q} = \pi w'(h_0^*) \theta l^*(\theta)$$

⇒ With complete insurance markets **all wedges are zero**.  
In this talk say: 'there is no scope for policy intervention'.

# The Bond Economy

- Assume that  $y$ ,  $\tilde{\theta}$ ,  $l$  and period 1 consumption all unobservable
- Agents cannot be insured against shocks (**self-insurance**)

$$\begin{aligned} \max_{h_0, k_0, l} \quad & u(y_0 - h_0 - qk_0) + \beta\pi [u(y + k_0) - v(l)] + \beta(1 - \pi)u(k_0) \\ \text{s.t.} \quad & y = w(h_0)\theta l \end{aligned}$$

- Optimal choice of  $k_0$  (Euler Equation):

$$qu'(c_0 - h_0) = \beta \sum_{\theta} \pi_{\theta} u'(c(\theta))$$

- Labor supply:

$$\theta w(h_0)u'(c(\theta)) = v'(l(\theta)), \quad l(0) = 0.$$

## Bond Economy II: Policy Predictions

- HC investment margin (HC is a 'bad' asset):

$$\frac{u'(c_0 - h_0)}{\beta u'(c(\theta))} = \pi(h_0)w'(h_0)\theta l(\theta) > \frac{1}{q}$$

- Note: uncertainty reduces the level of HC investment ( $h_0 < h_0^*$ ) and tends to increase  $k_0$  (precautionary savings).
- A tax on  $k_0$  might increase  $h_0$  as it would a HC subsidy
- In fact, there is again no scope for government intervention.
- All private and social margins coincide (constrained efficient):  
Exogenously incomplete markets & no pecuniary externalities.

# Endogenous Insurance Markets

## Observable HC

- $y_0$ ,  $y$ ,  $h_0$ , savings, and consumption in period 1 are **observable**.
- $\tilde{\theta}$  and  $l$  are not.

$$\max \quad u(c_0 - h_0) + \beta\pi [u(c(\theta)) - v(l(\theta))] + \beta(1 - \pi)u(\underline{c})$$

subject to

$$y_0 - c_0 + q\pi [w(h_0)\theta l(\theta) - c(\theta)] - q(1 - \pi)\underline{c} \geq 0; \quad (\lambda)$$

$$u(c(\theta)) - v(l(\theta)) \geq u(\underline{c}) \quad (\mu)$$

- **First-Best rule for HC investment**

$$\pi w'(h_0)\theta l(\theta) = \frac{1}{q}.$$

## Intuition of the First-Best rule for HC

- The social cost of investment is not distorted by incentives:

$$u'(c_0 - h_0) = \lambda$$

- The direct returns of  $h_0$  are fully internalized by the insurer which gives in exchange an allocation:  $q\lambda\pi w'(h_0)\theta I(\theta)$
- Social margin is not distorted by incentives:  $h_0$  is 'neutral' to the ex-post incentives for the insurer.  
In general, the multiplicative-separable form  $w(h_0)\theta$  matters.

Q: What does the first best rule mean for policy?

## Private Margins

- Again, would a private agent be happy to remain with the stated allocation?
- Labor margin is aligned to social margin (no-distortion-at-the-top)
- Some private margins are distorted (**Wedges**)

1. **Savings are discouraged** (complement to shirking):

$$qu'(c_0 - h_0) < \beta [\pi u'(c(\theta)) + (1 - \pi)u'(\underline{c})]$$

2. **Subsidize HC** (complement to working):

- Expected Return:

$$\pi w'(h_0)\theta l(\theta) = \frac{1}{q}$$

- Risk-adjusted private cost:

$$\frac{u'(c_0 - h_0)}{\beta u'(c(\theta))} > \frac{1}{q}$$

## Unobservable HC

- $y_0$ ,  $y$ , savings, and consumption in period 1 are observable.
- $\tilde{\theta}$  and  $h_0, l_1$  are **not observable**.

$$\max u(c_0 - h_0) + \beta\pi \left[ u(c(\theta)) - v\left(\frac{y(\theta)}{w(h_0)\theta}\right) \right] + \beta(1 - \pi)u(\underline{c})$$

subject to

$$y_0 - c_0 + q\pi [y(\theta) - c(\theta)] - q(1 - \pi)\underline{c} \geq 0; \quad (\lambda)$$

$$u(c_0 - h_0) + \beta\pi \left[ u(c(\theta)) - v\left(\frac{y(\theta)}{w(h_0)\theta}\right) \right] + \beta(1 - \pi)u(\underline{c}) \quad (\mu)$$

$\geq u(c_0) + \beta u(\underline{c})$  under-invest and lie:  $\hat{h}_0 = 0$  and  $\hat{\theta} = 0$ .

$$u'(c_0 - h_0) = \pi\beta u'(c(\theta))w'(h_0)\theta l(\theta) \quad (\text{slack})$$



## Results and Intuitions

- It is optimal to have HC paying a positive premium ('second best'  $h_0$  is below first best rule)

$$\pi w'(h_0)\theta l(\theta) > \frac{1}{q}.$$

- In this problem, the cost of  $h_0$  is affected by incentives:

$$u'(c_0 - h_0)(1 + \mu) = \lambda$$

- $h_0$  is now reduced -  $u'(c_0 - h_0)$  hence increases - to discourage the agent to deviate: under-invest and lie.

Q: What about Private Margins?

1. HC private and social margin coincide by construction;
2. Savings are again discouraged:

$$qu'(c_0 - h_0) < \beta [\pi(h_0)u'(c(\theta)) + (1 - \pi(h_0))u'(\underline{c})]$$

# Summary

- Economies with different **informational frictions**:
  1. Complete insurance markets (First-Best);
  2. The Bond economy (self-insurance);
  3. Imperfect insurance with observable HC;
  4. Imperfect insurance with hidden HC investment.
- We focused on **social margins compared to F-B** and **wedges**
- In 2. social margins differ from that of 1. (F-B). But in both economies there is no case for policy intervention (wedges=0)
- In 3. & 4. **savings are always discouraged** while **HC should be (weakly) subsidized** (positive vs negative wedges).
- In 3. social returns follow a First-Best rule, while in 4. HC investment is below the First-Best rule (social margins are 'distorted' away from First-Best rules as HC investment interacts with incentive constraints).

## Discussion

- ① Allowing for endogenous capital returns:  $k_0$  always follows first best rule

$$\frac{1}{q} = f'(k_0^*)$$

- ② This talk was **not on whether we should change existing policies**:

- We do not know what are the existing markets (empirical question)
- Policy reforms are quantitative questions.

- ③ **Heterogeneous returns**: If type is partially known in advance by the agent and  $h_0$  is observable, we have 'tagging' on an endogenous variable.

- ④ What about income taxation and HC? (endogenous weights)

- ⑤ What about hidden assets? (regressive taxation)